

**Homework 6. Due Thursday Nov. 22.**

1. **(10 pts)** Show that the Laplacian eigenmap to  $\mathbb{R}^m$  is the solution to the following optimization problem:

$$\sum_{i,j} k_{ij} \|y_i - y_j\|_2^2 = \text{tr}(Y^\top LY) \rightarrow \min \quad \text{subject to} \quad Y^\top QY = I, \quad Y^\top Q1_{n \times 1} = 0. \quad (1)$$

Here,  $y_i$ 's are columns of  $Y$ , and  $Y$  is  $n \times m$ .