

## Stat 430 Fall 2008 Sample Test Problems

The sample problems on the Fall 2006 sample test are all of the type I said in class I might ask this year.

Of the sample problems on the sample test from 2001, the parts of question II [parts c, e,f] which are based on the multiple regression output are not in scope for this year's mid-term because we have not covered any multiple regression topics yet.

Here are a few more sample problems appropriate for this year's test.

(A). Suppose that you have a SAS dataset ABCdat.sas7bdat in your home directory with three numeric columns named A, B, and C. Explain clearly, either by writing SAS code or by verbally summarizing the SAS data-steps and PROC's you would use to find

- (i) how many records have at least one missing column entry, and
- (ii) the mean of C and the correlation of variables A and B over all records which have no missing values.

(B). Four vectors  $\mathbf{y}$ ,  $\mathbf{x}$ ,  $\mathbf{w}$ , and  $\mathbf{e}$  of dimension 20 have inner-product values  $\mathbf{w}'\mathbf{e} = \mathbf{x}'\mathbf{e} = 0$  along with

$$\mathbf{x}'\mathbf{1} = \mathbf{w}'\mathbf{1} = \mathbf{e}'\mathbf{1} = 0, \quad \mathbf{x}'\mathbf{x} = 5, \quad \mathbf{w}'\mathbf{w} = 10, \quad \mathbf{x}'\mathbf{w} = 5, \quad \mathbf{e}'\mathbf{e} = 6$$

and the vector  $\mathbf{y}$  is related to the other vectors by:

$$\mathbf{y} = 2\mathbf{x} + \mathbf{w} + \mathbf{e}$$

- (a) Find  $s_x^2$ ,  $s_y^2$ , and the sample correlation  $\hat{\rho}_{yx}$  of  $\mathbf{y}$  on  $\mathbf{x}$ .
- (b) Find an expression for the residuals of  $\mathbf{y}$  and of  $\mathbf{x}$  from their simple linear regressions on  $\mathbf{w}$ .
- (c) Find the (sample) partial correlation of  $\mathbf{y}$  on  $\mathbf{x}$  after removing the effect of  $\mathbf{w}$ .

(C). Define the following statistical concepts for a univariate column  $x_1, \dots, x_n$  of data values:

- (i) *empirical distribution function*.
- (ii) *upper quartile* or *75th percentile*.
- (iii) *scaled relative frequency histogram* on the range (a,b) (assumed to contain all of the data points).

(D). Suppose you have a numeric column named `Y` in a SAS dataset `XY-dat.sas7bdat`, together with a group-label column `GP` which takes on values 1 and 2. If you wanted to explore how the distribution of `Y`-values differs between the `GP=1` and `GP=2` groups, explain how to get information on this question using each of the following SAS PROC's, saying as clearly as possible what options you would use and what you would look for in the output and what it could tell you:

- (i) PROC UNIVARIATE or PROC BOXPLOT side-by-side boxplots for `Y`-values for the two `GP`-defined groups.
- (ii) PROC FREQ after breaking `Y` down into categories `YCATG` defined by intervals of values in a `DATA` step.
- (iii) PROC TTEST on the two `GP`-defined samples of `Y` values.